

# Alignment of graphene nanoribbons by an electric-field

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## Abstract

In this paper, we develop an analytical approach to predict the field-induced alignment of cantilevered graphene nanoribbons. This approach is validated through molecular simulations using a constitutive atomic electrostatic model. Our results reveal that graphene's field-oriented bending angle is roughly proportional to the square of field strength or the graphene length for small deformations, while is roughly independent of graphene width. The effective bending stiffness and the longitudinal polarizability are also found to be approximately proportional to the square of graphene length. Compared with carbon nanotubes, graphene nanoribbons are found to be more mechanically sensitive to an external electric field.

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## 1. Introduction

Graphene's electronic gap tunable in external electromagnetic fields [1, 2, 3, 4] makes it promising for a number of potential applications in nanoelectronic devices [5, 6, 7]. Since graphene is often supposed to work in a transverse electric field in such devices and its electronic transport prop-

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6 erties strongly depend on its atomic structure [8, 9, 10], understanding of  
 7 graphene’s mechanical behaviors in an electric field is of great importance for  
 8 nanoelectromechanical systems based on graphene. However, as a novel is-  
 9 sue, the mechanical response of graphene to an external field has not yet been  
 10 reported up to date. *How does graphene deform in response to applied elec-*  
 11 *tric fields?* To answer this question, we developed a simple model to predict  
 12 the field-induced alignment of cantilevered graphene nanoribbons (GNRs),  
 13 demonstrating the coupling between the graphene’s field-induced bending,  
 14 molecular stiffness and electric polarization. This model is validated through  
 15 molecular simulations, in view of the difficulties of experimental quantifica-  
 16 tion of this electromechanical effects in nanoscale.

17 If a thin nanostructure is brought into an electric field, electric polariza-  
 18 tion effects will induce a moment of force, which tends to orient the nanos-  
 19 tructure toward the field direction [11]. This moment will make the nanos-  
 20 tructure bent if one end of the nanostructure is fixed on a substrate (see  
 21 Fig. 1). This alignment has been observed on carbon nanotubes (CNTs) in  
 22 early experiments [12], and then exploited in designing nanorelays [13] and  
 23 field emission devices [14]. As can be expected in view of the large similarity  
 24 in their atomic structures and mechanical properties [15], graphene nanorib-  
 25 bons (GNRs) should exhibit similar mechanical behaviors in an electric field.  
 26 Furthermore, unlike CNTs, graphene exhibits strong mechanical anisotropy  
 27 in its transverse direction, with a lateral stiffness about 30 times lower than  
 28 that in the longitudinal direction [16, 17]. This high lateral structural flexi-  
 29 bility makes GNRs ideal field-sensing materials in resonators [5], transistors  
 30 [18] or sensors [19].

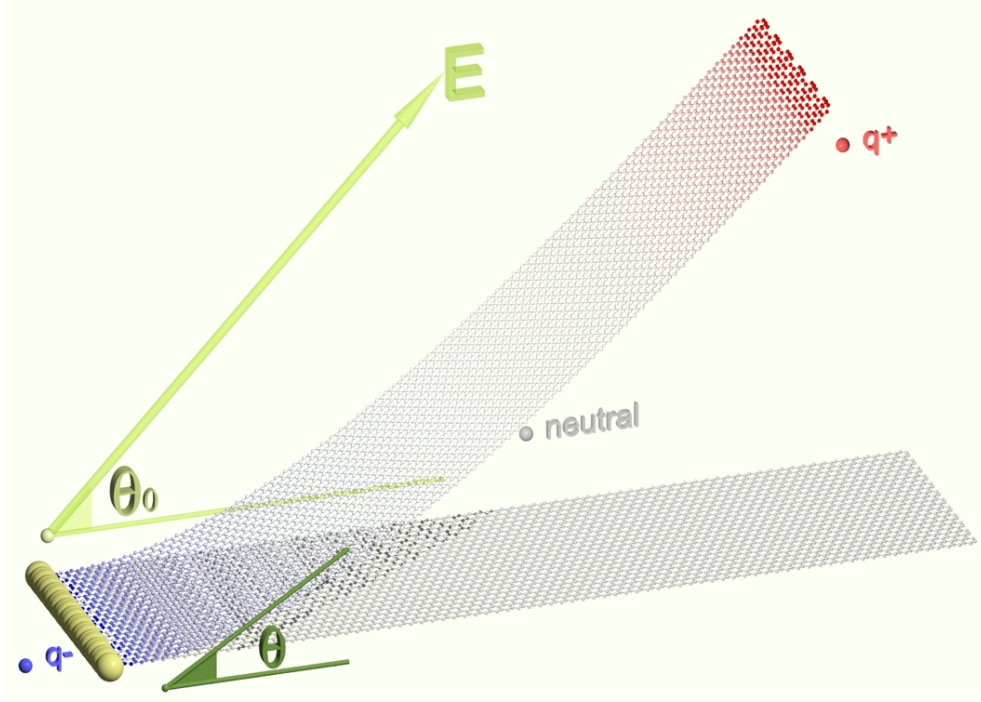


Figure 1: Alignment of a cantilevered GNR ( $L \approx 20\text{nm}$ , periodic in width direction) to an electric field  $E = 0.3\text{V/nm}$ . The color scale of atoms represents the intensity of induced charges  $q$ .

## 31 2. Simulations

32 In this work, molecular simulations were performed to compute equilib-  
 33 rium structures of cantilevered GNRs in an electric field, using an energy  
 34 optimization method (full details of the simulation techniques can be found  
 35 elsewhere [20, 21]). The principle of this method is to minimize the potential  
 36 energy of each atom, which consists of an internal potential due to the C-C  
 37 chemical bonds and the long-range interaction, and of an external potential  
 38 induced by applied electrostatic fields. The internal potential is calculated  
 39 using the adaptive interatomic reactive empirical bond order (AIREBO) po-

40 tential function [22], which has been used in recent studies on mechanical  
41 properties of CNTs [23] and GNRs [24]. The external potential describes  
42 the electrostatic interaction between the charges, the dipoles and the ex-  
43 ternal field, it is computed using an atomic charge-dipole interacting model  
44 [25, 27, 28], which has been validated through charge-injection experiments  
45 using an atomic force microscope [29].

### 46 3. Modeling

47 The main reason of the field-induced alignment of a GNR is the effect  
48 of electric polarization, by which a quantity of positive and negative charges  
49 are shifted to opposite directions in graphene (see Fig. 1). A moment of  
50 a force pair arises from the electrostatic interactions between the field and  
51 the induced charges, and makes the graphene bent into the field direction.  
52 This field-driving moment highly correlated with the GNR's polarizability is  
53 resisted by the mechanical lateral stiffness of graphene, due to the repulsive  
54 interactions between  $\pi$  electrons and the rotation of  $\sigma$  bonds. Considering  
55 the correlations between the electric polarizability, the bending stiffness, and  
56 the geometry of GNRs, the curvature  $\omega$  of a cantilevered GNR in an electric  
57 field can be calculated as follows:

$$\omega = \frac{M}{K} = \frac{E^2(\alpha_{//} - \alpha_{\perp}) \sin [2(\theta_0 - \theta)]}{2K} \quad (1)$$

58 where  $M$  is the bending moment induced by the electric polarization [30],  
59  $K$  denotes the effective bending stiffness of GNR,  $L$  stands for the graphene  
60 length,  $\theta$  is the deflection angle of GNR,  $E = |\mathbf{E}|$ , and  $\theta_0$  represent the  
61 strength and the direction of the electric field, respectively,  $\alpha_{//}$  and  $\alpha_{\perp}$  stand

62 for the longitudinal and the transverse molecular polarizabilities of GNR,  
 63 respectively.  $\theta$  is defined as the angle between the initial axis of graphene  
 64 and the vector from one graphene end to another after deformation. Since  
 65 the curvature  $\omega$  can be approximated as  $\omega = 2\theta/L$  and usually  $\alpha_{//} \gg \alpha_{\perp}$ ,  
 66 the governing equation can therefore be written as

$$\theta \approx \frac{LE^2\alpha_{//}^* \sin[2(\theta_0 - \theta)]}{4K^*} \quad (2)$$

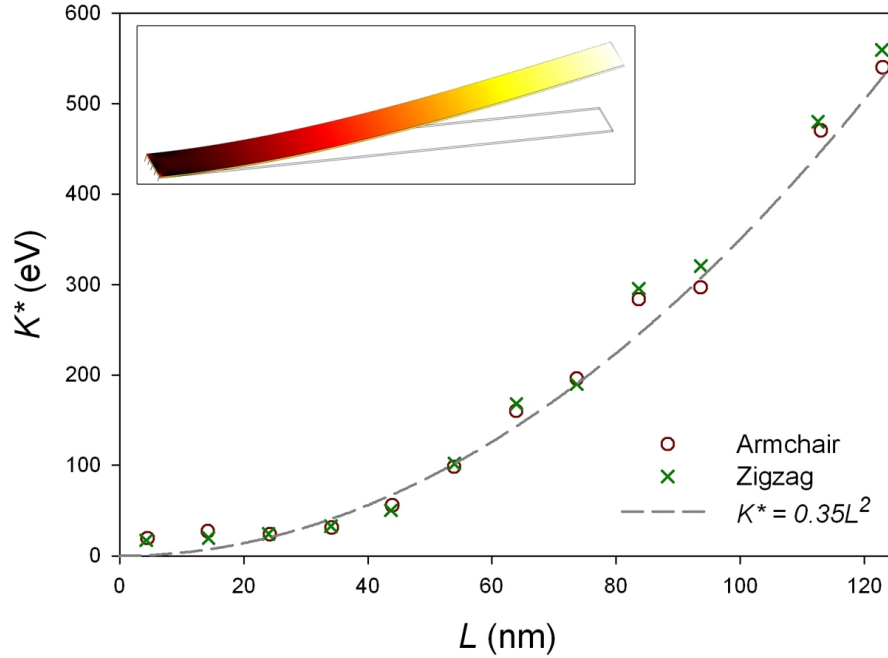


Figure 2:  $K^*$  vs  $L$  from simulations, in which the periodic condition was applied in width direction. Symbols show simulation data and the dashed line stands for a fitting curve. The inset shows the main stress distribution in a curved graphene.

67 where  $\alpha_{//}^*$  and  $K^*$  stand for the quantities of  $\alpha_{//}$  and  $K$  per unit width,  
 68 respectively. In Eq. 2, the parameter representing the mechanical resistance

69 of a GNR is the effective bending stiffness  $K$ . Here its values were directly  
 70 computed from atomic simulations by applying a mechanical force at the  
 71 free end of the GNRs in absence of electric field, instead of using a conven-  
 72 tional formula for macroscopic continuous media as the product of the elastic  
 73 modulus and the area moment of inertia, in order to avoid the problem of  
 74 definition of the wall-thickness of a one-single-atom thick layer [31]. Note  
 75 that previous studies showed that the bending stiffness of a CNT is an *inde-*  
 76 *pendent parameter* not necessarily related to the representative thickness by  
 77 the classic formula [32]. Our simulation results show that  $K^*$  is about 20eV  
 78 when  $L < 20\text{nm}$  and is roughly proportional to  $L^2$  when GNRs get longer  
 79 (see Fig. 2). These simulation data can be fitted using a simple equation as

$$K^* = AL^2 \quad (L > 20\text{nm}) \quad (3)$$

80 where  $A = 0.35\text{eV}\cdot\text{nm}^{-2}$  for GNRs with either armchair or zigzag edges.  
 81 For comparison, we also calculated the effective bending stiffness of CNTs.  
 82 It is found that the value of  $K$  of a GNR ( $L \approx 10\text{nm}$ ,  $K \approx 19.2\text{eV}\cdot\text{nm}$ )  
 83 is about 20 times smaller than that of a (5, 5) CNTs of the same length  
 84 ( $K \approx 570\text{eV}\cdot\text{nm}$ ). This large difference in the transverse (lateral) stiffness  
 85 implies that the alignment of GNRs can be much more significant than that  
 86 of CNTs for a given magnitude of electric polarization.

87 Another important parameter in Eq. 2 is  $\alpha_{//}^*$ . Its value was determined  
 88 using electrostatic simulations based on the atomic charge-dipole model [25].  
 89 In these simulations, the value of  $\alpha_{//}^*$  was calculated from the definition  
 90  $\vec{p} = \vec{E}\vec{\bar{\alpha}}$ , where  $\vec{\bar{\alpha}}$  is the the matrix of molecular polarizability,  $\vec{p}$  and  $\vec{E}$   
 91 stand for the vectors of the induced molecular dipole (see Fig. 3 (a)) and the

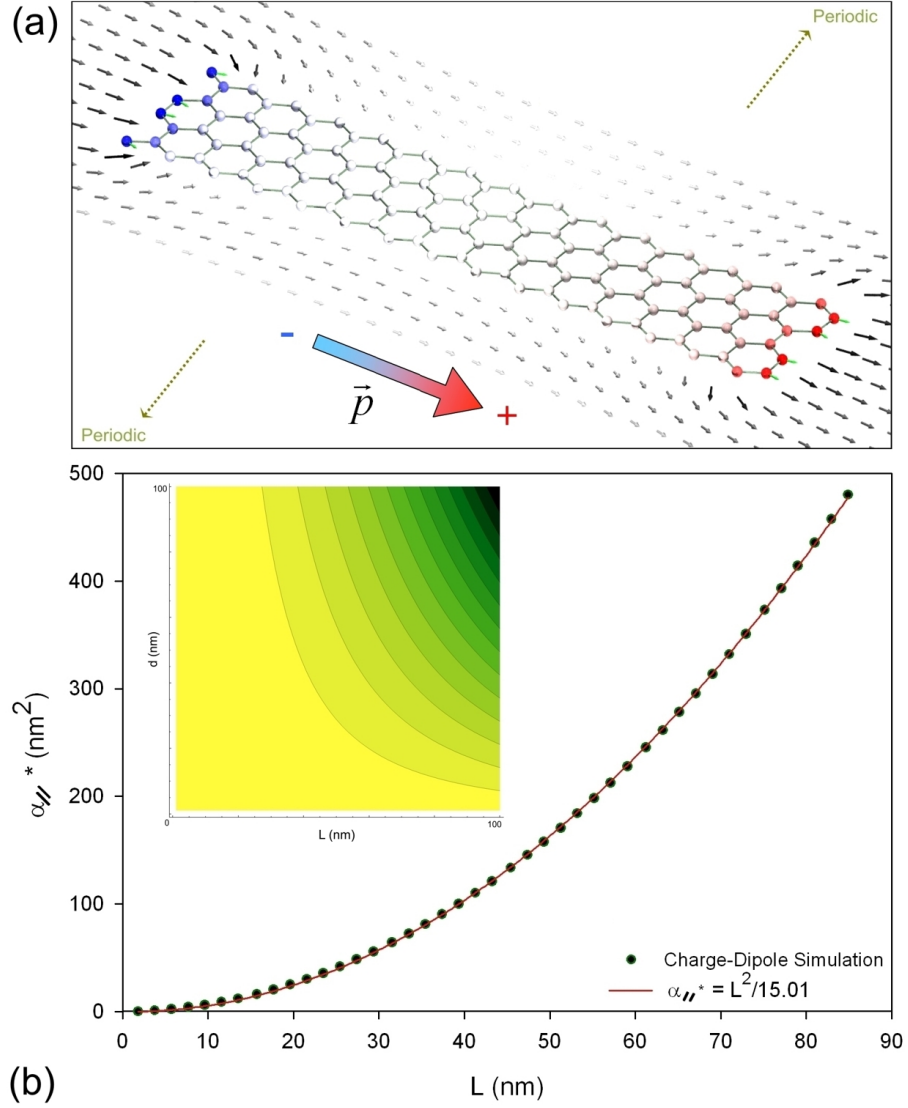


Figure 3: (a) Polarization of a GNR in a longitudinal electric field. Color scale of atom represents the intensity of induced charges. Dark arrows show the electric field around the graphene. (b) Longitudinal polarizability per 1nm width  $\alpha_{//}^*$  vs  $L$ . Circles denote simulation data and the dashed line stands for a numerically fitting curve. Coupled dependence of  $\alpha_{//}^*$  on  $L$  and width  $d$  is shown in the inset, in which the color scale represents the amplitude of  $\alpha_{//}^*$ .

92 applied electric field, respectively. As shown in Fig. 3 (b), our simulation  
 93 results suggest that  $\alpha_{//}^*$  is roughly proportional to  $L^2$ .

$$\alpha_{//}^* = \frac{L^2}{B} \quad (L > 6nm) \quad (4)$$

94 where  $B = 15.01$  is a constant for either armchair or zigzag GNRs, since  
 95 no large difference has been found between  $\alpha_{//}^*$  of these two types of graphene.  
 96 Since Eq. 4 shows a typical metallic behavior of graphene, we note that  $\alpha_{//}^*$  of  
 97 semi-conducting graphene (minimum lateral dimension  $< 6nm$  [26]) should  
 98 hold a linear relationship with  $L$ . Putting the empirical fits to  $\alpha_{//}$  and  $K^*$   
 99 into Eq. 2, we finally obtain the governing equation of the electrostatic  
 100 alignment of GNRs as follows:

$$\theta = \frac{E^2 L \sin [2(\theta_0 - \theta)]}{C} \quad (L > 20nm) \quad (5)$$

101 where  $C = 4AB \approx 21eV \cdot nm^{-2}$ . We note that, since the geometry periodic  
 102 condition was applied in the width direction in our calculations, we effectively  
 103 simulated graphene of infinite width. Thus, the edge disorder effects on  
 104 structural [33] and mechanical properties [24] of graphene were neglected.

#### 105 4. Results and discussions

106 We can see from Eq. 5 that, in small deformation region,  $\theta$  is roughly  
 107 proportional to  $E^2$ ,  $\sin \theta_0$  or  $L$ . In Fig. 4, we plot data of the alignment  
 108 ratio  $\theta/\theta_0$  as a function of  $E$  from molecular simulations in which periodic  
 109 geometry condition is applied in width direction. A quantitative agreement  
 110 was obtained between the simulation data and the analytical prediction using  
 111 Eq. 5. The main inaccuracy can be considered to be contributed from the



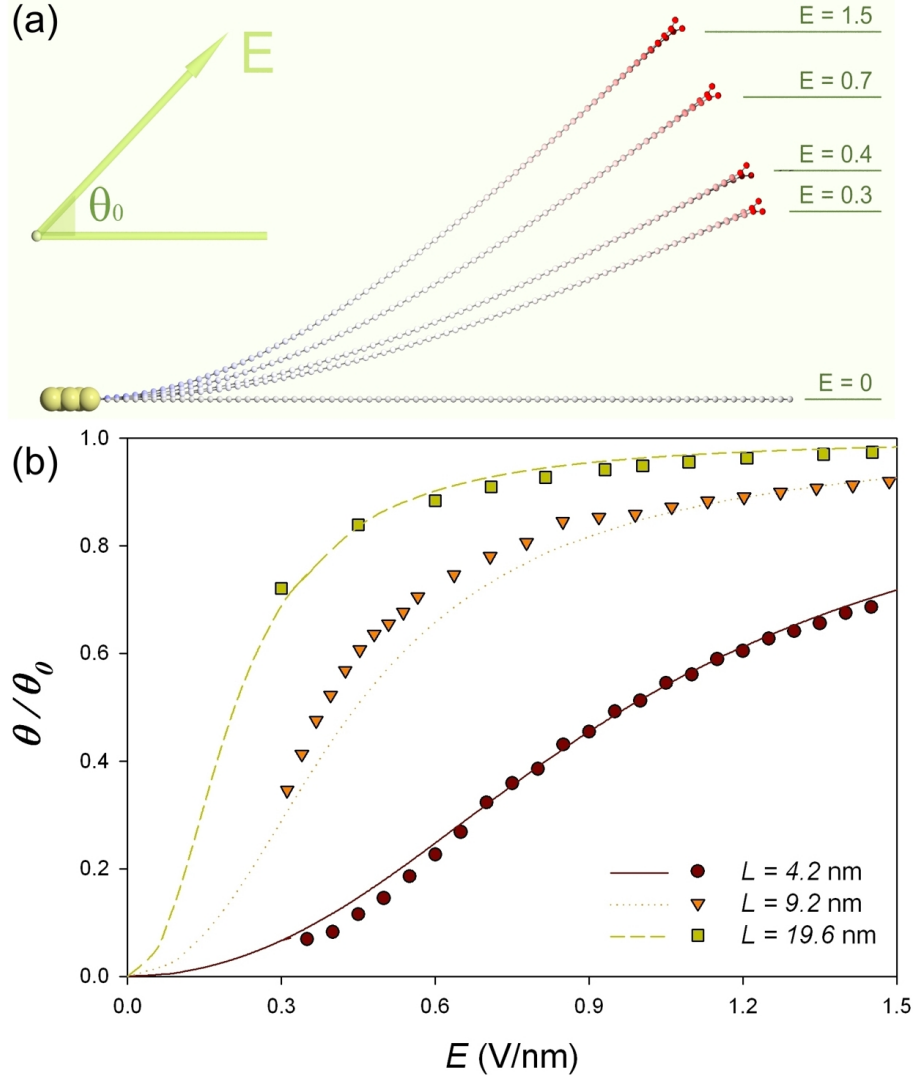


Figure 4: (a) Cross sections of a GNR ( $L \approx 9.2$  nm) in different electric fields  $\mathbf{E}$  ( $\theta_0 = \pi/4$ ), (a video recording file is available on line). (b) Alignment ratio  $\theta/\theta_0$  versus the field strength  $E$  for GNRs of different lengths. The symbols represent numerical data and the lines stand for results predicted by analytical model.

112 geometry approximations and the possible slight change of polarizability due  
 113 to the curvature of graphene. We can see that the S-shaped curve of  $\theta/\theta_0$   
 114 tends to be flat near the maximal value 1 when the GNRs are well aligned  
 115 to the field direction. In such a case that  $\sin[2(\theta_0 - \theta)] \approx 2(\theta_0 - \theta)$ , Eq. 5  
 116 can be simplified to

$$\frac{\theta}{\theta_0} \approx 1 - \frac{C}{C + 2E^2L} \quad (6)$$

117 for large deformation. Compared with GNRs in same sizes, CNTs were  
 118 found to be less flexible in an electric field, e.g., a (5,5) SWCNT ( $L \approx 10\text{nm}$ )  
 119 can be bent to  $\theta/\theta_0 \approx 0.4$  in an electric field ( $E \approx 2.0\text{V/nm}$  and  $\theta_0 = \pi/4$ ),  
 120 while required field strength for producing the same amplitude of alignment  
 121 for a GNR with the same width and length is about 7 times smaller ( $E \approx$   
 122  $0.3\text{V/nm}$ ). Analysis on the amplitudes of induced polarization in a GNR and  
 123 a CNT shows that this difference is mainly due to the fact that the bending  
 124 stiffness of the GNR is much lower than that of the CNT. Furthermore,  
 125 we can predict that a multi-layered graphene should be less sensitive to an  
 126 electric field than a single-layered one is, because of the electric screening  
 127 effects and the friction between the layers [20].

## 128 5. Conclusion

129 In conclusion, we have developed an analytical model to predict the align-  
 130 ment of cantilevered GNRs to an electrostatic field. Parameters used in this  
 131 model such as the polarizability and the bending stiffness were determined  
 132 from numerical fits to the data of simulations using an atomic electrostatic  
 133 charge-dipole model and an empirical pseudo-chemical potential. This model

134 showed that the alignment angle roughly follows a linear relationship with  
 135 the square of field strength and the graphene length when the deformation  
 136 remains small. It was also found that, for GNRs with either armchair or  
 137 zigzag edges, their effective bending stiffness and longitudinal polarizability  
 138 are both approximately proportional to the square of graphene length. Com-  
 139 parison showed that a GNR can be more easily oriented to electric fields than  
 140 a CNT does, due to the GNR's low transverse bending stiffness.

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